

Name : _____

Grade : VIII

Subject : Mathematics

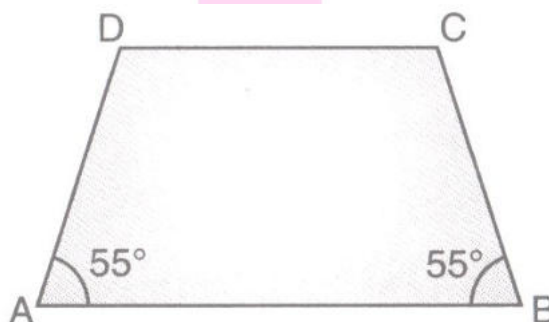
Chapter : 3. Understanding Quadrilaterals

Objective Type Questions

1 Marks.

I. Multiple choice questions

- What is the sum of all the angles of a pentagon? [NCERT Exemplar]
 a. 180° b. 360° c. 540° d. 720°
- The number of sides of a regular polygon where each exterior angle has a measure of 45° is : [NCERT Exemplar]
 a. 8 b. 10 c. 4 d. 6
- Sum of the interior angles of a regular polygon of n sides is : [NCERT Exemplar]
 a. $n \times 90^\circ$ b. $(n - 2) \times 90^\circ$ c. $n \times 180^\circ$ d. $(n - 2) \times 180^\circ$
- In the trapezium ABCD, the measure of $\angle D$ is [NCERT Exemplar]
 a. 55° b. 115° c. 135° d. 125°



- PQRS is a square. PR and SQ intersect at O. Then $\angle POQ$ is a [NCERT Exemplar]
 a. Right angle b. Straight angle c. Reflex angle d. Complete angle
- Which of the following is not true for an exterior angle of a regular polygon with n sides ? [NCERT Exemplar]
 a. Each exterior angle = $\frac{360^\circ}{n}$ b. Exterior angle = $180^\circ - \text{interior angle}$
 c. $n = \frac{360^\circ}{\text{exterior angles}}$ d. Each exterior angle = $\frac{(n-2) \times 180^\circ}{n}$

1. c	2. a	3. d	4. d	5. a	6. d
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II. Multiple choice questions

1. Which of the following is a property of a parallelogram?

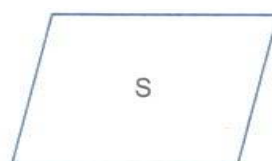
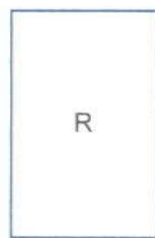
- a. Opposite sides are parallel
- b. The diagonals bisect each other at right angles
- c. The diagonals are perpendicular to each other
- d. All angles are equal

2. Which of the following figures satisfy the following properties? [NCERT Exemplar]

— All sides are congruent.

— All angles are right angles.

— Opposite sides are parallel.



- a. P b. Q c. R d. S

3. A quadrilateral whose all sides, diagonals and angles are equal is

[NCERT Exemplar]

- a. square
- b. trapezium
- c. rectangles
- d. rhombus

4. The sum of all exterior angles of a triangle is

- a. 180°
- b. 360°
- c. 540°
- d. 720°

5. If the diagonals of a quadrilateral are equal and bisect each other, then the quadrilateral is a

[NCERT Exemplar]

- (a) rhombus
- (b) rectangle
- (c) square
- (d) parallelogram

6. How many diagonals does a hexagon have? [NCERT Exemplar]

- (a) 9
- (b) 8
- (c) 2
- (d) 6

7. What is the maximum number of obtuse angles that a quadrilateral can have?

[NCERT Exemplar]

- (a) 1
- (b) 2
- (c) 3
- (d) 4

8. How many non-overlapping triangles can we make in a n-gon (polygon having n sides), by joining the vertices?

[NCERT Exemplar]

- (a) $n - 1$
- (b) $n - 2$
- (c) $n - 3$
- (d) $n - 4$

9. If two adjacent angles of a parallelogram are $(5x - 5)^\circ$ and $(10x + 35)^\circ$ then the ratio of these angles is

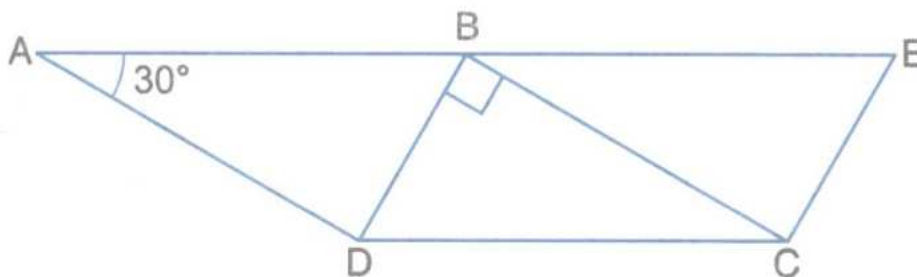
[NCERT Exemplar]

- (a) 1 : 3
- (b) 2 : 3
- (c) 1 : 4
- (d) 1 : 2

10. In Fig., ABCD and BDCE are parallelograms with common base DC. If $BC \perp BD$

then $\angle BEC =$

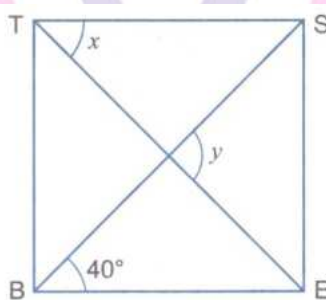
[NCERT Exemplar]



- (a) 60° (b) 30° (c) 150° (d) 120°

11. In Fig., BEST is a rhombus. Then the value of $y - x$ is

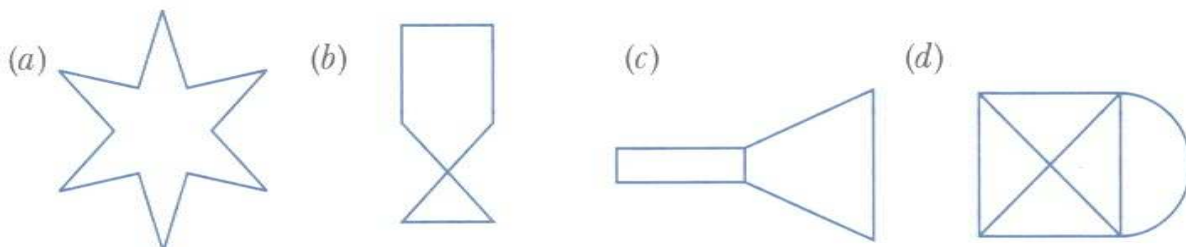
[NCERT Exemplar]



- (a) 40° (b) 50° (c) 20° (d) 10°

12. The closed curve which is also a polygon is

[NCERT Exemplar]



13. The sum of angles of a concave quadrilateral is

[NCERT Exemplar]

- (a) more than 360° (b) less than 360°
(c) equal to 360° (d) twice of 360°

14. Which of the following can never be the measure of exterior angle of a regular polygon?

(Hint: Measure of exterior angle of a regular polygon should be a multiple of 360)

[NCERT Exemplar]

- (a) 22° (b) 36° (c) 45° (d) 30°

15. PQRS is a trapezium in which $PQ \parallel SR$ and $\angle P = 130^\circ$, $\angle Q = 110^\circ$. Then $\angle R$ is equal to

[NCERT Exemplar]

- (a) 70° (b) 50° (c) 65° (d) 55°



16. The number of sides of a regular polygon whose each interior angle of 135° is

[NCERT Exemplar]

- (a) 6 (b) 7 (c) 8 (d) 9

17. What is the sum of all angles of a hexagon? [NCERT Exemplar]

- (a) 180° (b) 360° (c) 540° (d) 720°

18. The angle between the two altitudes of a parallelogram through the same vertex of an obtuse angle of the parallelogram is 30° . The measure of the obtuse angle is

[NCERT Exemplar]

- (a) 100° (b) 150° (c) 105° (d) 120°

1. (a)	2. (b)	3. (a)	4. (b)	5. (b)	6. (a)	7. (c)	8. (b)	9. (a)
10. (a)	11. (a)	12. (a)	13. (c)	14. (a)	15. (a)	16. (c)	17. (d)	18. (b)

I. Fill in the blanks

- The diagonals of a rhombus bisect each other at _____. [NCERT Exemplar]
- The sum of interior angles of a polygon of n sides is _____ right angles. [NCERT Exemplar]
- All sides of a _____ are equal and all angles are right angles. [NCERT Exemplar]
- If all sides of a quadrilateral are equal, it is a _____. [NCERT Exemplar]
- A square has sides of equal length and angles of equal measure, so it is _____ a polygon. [NCERT Exemplar]

1. Right angles	2. $2n - 4$	3. Square	4. Rhombus	5. Regular
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I. True or False

- All rectangles are parallelograms. [NCERT Exemplar]
- All squares are rectangles. [NCERT Exemplar]
- All angles of a trapezium are equal. [NCERT Exemplar]
- All kites are squares. [NCERT Exemplar]
- Sum of all the angles of a quadrilateral is 180° . [NCERT Exemplar]
- If diagonals of a quadrilateral are equal, it must be a rectangle. [NCERT Exemplar]

1. True	2. True	3. False	4. False	5. False	6. False
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I. Very Short Answer Type Questions

1. Find the number of sides of a regular polygon, whose each exterior angle has a measure of 40° . [NCERT Exemplar]

Sol. Since, the given polygon is a regular polygon.

\therefore Its each exterior angle is equal.

\therefore Sum of all the exterior angles = 360°

\therefore Number of exterior angles = $\frac{360^\circ}{40^\circ}$

\Rightarrow Number of sides = 9

2. Each interior angle of a polygon is 108° . Find the number of sides of the polygon.

[NCERT Exemplar]

Sol. Since each interior angle = 108°

So, exterior angle = $180^\circ - 108^\circ = 72^\circ$

Number of sides = $\frac{360^\circ}{\text{exterior angle}} = \frac{360^\circ}{72^\circ} = 5$

3. The four angles of a quadrilateral are in the ratio 3 : 4 : 5 : 6. Find the angles.

[NCERT Exemplar]

Sol. Let angles be $3x, 4x, 5x, 6x$.

Thus, $3x + 4x + 5x + 6x = 360^\circ$, Since, sum of the angles of a quadrilateral is 360° .

So, $18x = 360^\circ$

or, $x = 20^\circ$

Thus, angles are $60^\circ, 80^\circ, 100^\circ, 120^\circ$.

4. Two adjacent angles of a parallelogram are in the ratio 4 : 5. Find their measures.

[NCERT Exemplar]

Sol. Let the angles be $4x$ and $5x$.

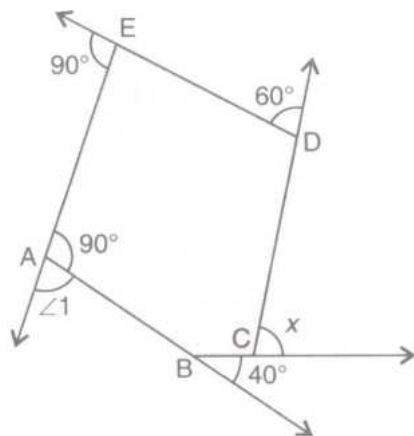
Then, $4x + 5x = 180^\circ$ $9x = 180^\circ$

$x = 20^\circ$

So, angles are $4 \times 20^\circ = 80^\circ$ and $5 \times 20^\circ = 100^\circ$.

5. Find x and $\angle 1$ in the following figure.

[NCERT Exemplar]



Sol. In the given figure $\angle 1 + 90^\circ = 180^\circ$ (linear pair)

$$\angle 1 = 90^\circ$$

Now, sum of exterior angles of a polygon is 360° .

Therefore, $x + 60^\circ + 90^\circ + 90^\circ + 40^\circ = 360^\circ$

$$x + 280^\circ = 360^\circ$$

$$x = 80^\circ$$

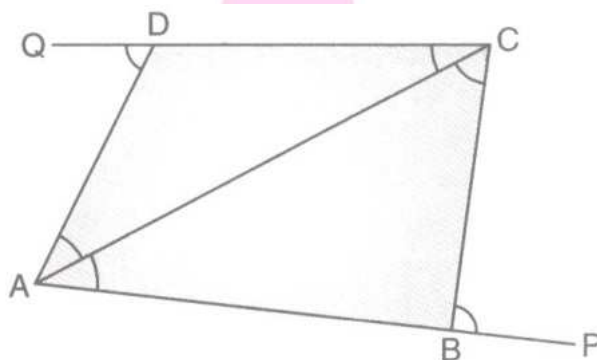
6. The sides AB and CD of a quadrilateral ABCD are extended to points P and Q respectively. Is $\angle ADQ + \angle CBP = \angle A + \angle C$? Give reason. [NCERT Exemplar]

Sol. Join AC, then

$$\angle CBP = \angle BCA + \angle BAC \text{ and}$$

$$\angle ADQ = \angle ACD + \angle DAC$$

(Exterior angles of triangles)

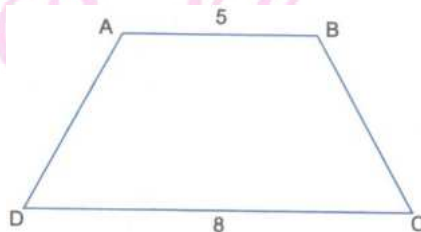


Therefore,

$$\begin{aligned} \angle CBP + \angle ADQ &= \angle BCA + \angle BAC + \angle ACD + \angle DAC \\ &= (\angle BCA + \angle ACD) + (\angle BAC + \angle DAC) \\ &= \angle C + \angle A \end{aligned}$$

II. Very Short Answer Type Questions

1. ABCD is a quadrilateral in which $AB = 5$ cm, $CD = 8$ cm and the sum of angle A and angle D is 180° . What is the name of this quadrilateral?



Sol. Since $\angle A + \angle D = 180^\circ$
 These are interior angles on the same side of transversal (AD).
 Therefore $AB \parallel DC$
 Hence, ABCD is a trapezium.

2. Two adjacent angles of a parallelogram are in the ratio 1 : 3. Find its angles.

[NCERT Exemplar]

Sol. Let the angles be x and $3x$.

$$\begin{aligned} \text{Then, } x + 3x &= 180^\circ \\ 4x &= 180^\circ \Rightarrow x = 45^\circ \end{aligned}$$

So, angles are 45° and $(3 \times 45^\circ)$ i.e., 135° .

3. A photo frame is in the shape of a quadrilateral with one diagonal longer than the other. Is it a rectangle? Why or why not?

[NCERT Exemplar]

Sol. No, it is not a rectangle. In a rectangle diagonals are equal.

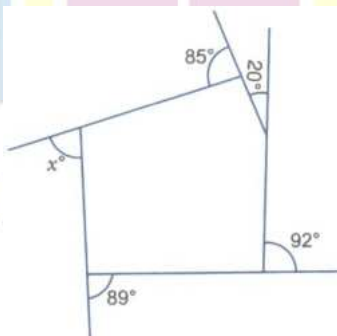
4. In Fig. 3.24, find the value of x .

[NCERT Exemplar]

Sol. Sum of all exterior angles $= 360^\circ$

$$x + 89^\circ + 92^\circ + 20^\circ + 85^\circ = 360^\circ$$

$$x + 286^\circ = 360^\circ \Rightarrow x = 360^\circ - 286^\circ = 74^\circ.$$





5. The point of intersection of diagonals of a quadrilateral divides one diagonal in the ratio 1 : 2. Can it be a parallelogram? Why or why not? [NCERT Exemplar]

Sol. No, it cannot be a parallelogram. Diagonals of parallelogram bisect each other i.e., in the ratio 1 : 1.

6. A playground in the town is in the form of a kite. The perimeter is 106 metres. If one of its sides is 23 metres, what are the lengths of other three sides?

Sol. A kite has two pairs of equal consecutive sides.

∴ One side = 23 m

Other side = 23 m

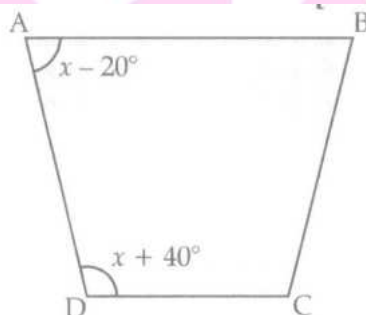
Sum of rest two sides = 106 — (23 + 23) = 60 m

Length of other two sides are 30 m and 30 m.

Hence, the length of other three sides are 23 m, 30 m and 30 m.

I. Short Answer Type Questions

1. Find the value of x in the trapezium ABCD given below. [NCERT Exemplar]



Sol. In the given trapezium ABCD, we have $AB \parallel CD$

Also, sum of interior angles A and D is 180° .

$$\therefore \angle A + \angle D = 180^\circ$$

$$(x - 20^\circ) + (x + 40^\circ) = 180^\circ$$

$$2x^\circ + 20^\circ = 180^\circ$$

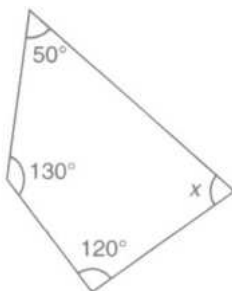
$$2x^\circ = 160^\circ$$

$$x^\circ = 80^\circ$$



2. Find the measure of angle x in the following figure :

[NCERT Exemplar]



Sol. The sum of interior angles of a quadrilateral = 360°

$$\therefore x + 120^\circ + 130^\circ + 50^\circ = 360^\circ$$

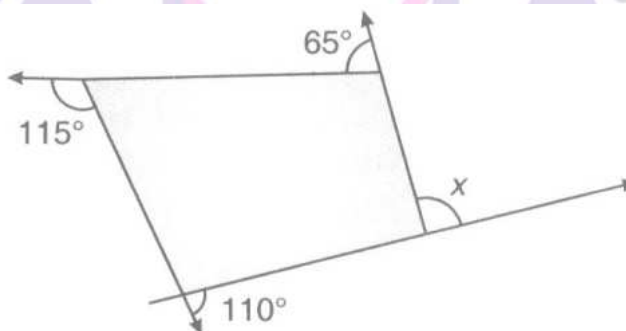
$$\therefore x + 300^\circ = 360^\circ$$

$$\therefore x = 360^\circ - 300^\circ$$

$$x = 60^\circ$$

3. Find the measure of x in the figure.

[NCERT Exemplar]



Sol. Sum of all the exterior angles of a quadrilateral = 360°

$$\therefore x + 65^\circ + 115^\circ + 110^\circ = 360^\circ$$

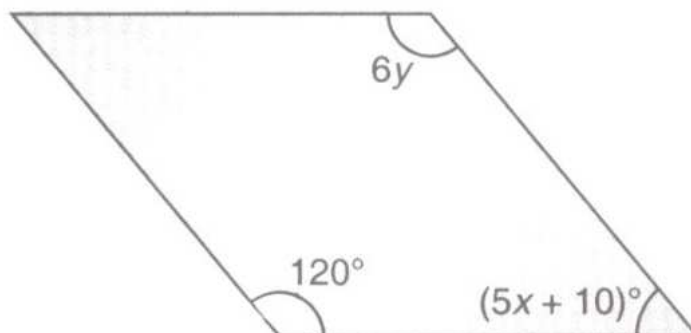
$$\therefore x + 290^\circ = 360^\circ$$

$$\text{or } x = 360^\circ - 290^\circ$$

$$\therefore x = 70^\circ$$

4. Find the values of x and y in the following parallelogram.

[NCERT Exemplar]



Sol. \therefore Opposite angles of a parallelogram are equal

$$\therefore 6y = 120^\circ \quad y = 20^\circ$$

$$\text{Now, } 5x + 10^\circ + 6y = 180^\circ$$

$$5x + 10^\circ + 6 \times 20^\circ = 180^\circ$$

$$5x = 180^\circ - 130^\circ$$

$$5x = 50^\circ$$

$$x = \frac{50^\circ}{5}$$

$$x = 10^\circ$$

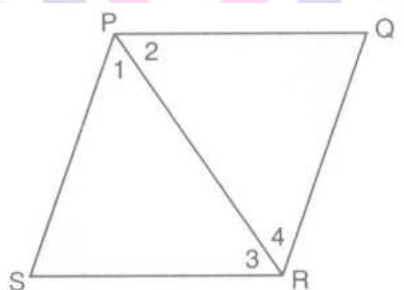
5. Find the measure of exterior angle of a regular pentagon and an exterior angle of a regular decagon. What is the ratio between these two angles. [NCERT Exemplar]

Sol. Exterior angle of a regular pentagon = $\frac{360^\circ}{5} = 72^\circ$

Exterior angle of a regular decagon = $\frac{360^\circ}{10} = 36^\circ$

Ratio between these two = $\frac{72^\circ}{36^\circ} = 2 : 1$

6. One of the diagonals of a rhombus and its sides are equal. Find the angles of the rhombus. [NCERT Exemplar]



Sol. Let PQRS be a rhombus such that its diagonal PR is equal to its side, that is, $PQ = QR = RS = PS = PR$. So, $\triangle PRS$ and $\triangle PQR$ are equilateral.

$\angle S = \angle Q = 60^\circ$ [Each angle of an equilateral triangle is 60° .]

and

$$\angle P = \angle 1 + \angle 2 = 60^\circ + 60^\circ = 120^\circ = \angle R$$

Hence, $\angle S = \angle Q = 60^\circ$ and $\angle P = \angle R = 120^\circ$

7. The ratio of exterior angle to interior angle of a regular polygon is 1 : 4. Find the number of sides of the polygon. [NCERT Exemplar]

Sol. Let the exterior angle of the polygon be x . Then, the interior angle of polygon = $180^\circ - x$. According to question,

$$\frac{x}{180^\circ - x} = \frac{1}{4}$$

or, $4x = 180^\circ - x$

or, $5x = 180^\circ$

or, $x = \frac{180^\circ}{5}$

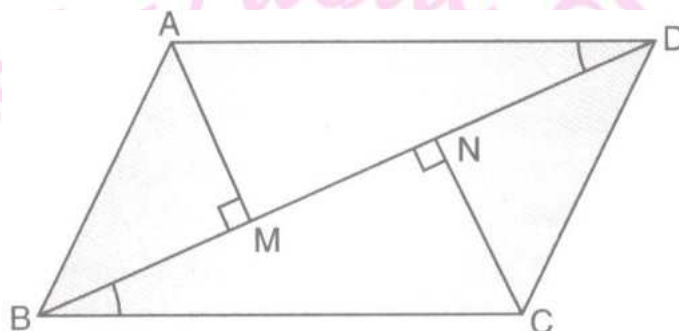
so, $x = 36^\circ$

$$\begin{aligned} \text{Number of sides of polygon} &= \frac{360^\circ}{\text{exterior angle}} \\ &= \frac{360^\circ}{36^\circ} = 10 \end{aligned}$$

8. If AM and CN are perpendiculars on the diagonal BD of a parallelogram ABCD,

Is $\triangle AMD \cong \triangle CNB$? Give reason.

[NCERT Exemplar]



Sol. In $\triangle AMD$ and $\triangle CNB$

$$AD = BC$$

(opposite side of parallelogram)

$$\angle DMB = \angle CNB = 90^\circ$$

$$\angle ADM = \angle NBC$$

($AD \parallel BC$ and BD is transversal)

So, $\triangle AMD \cong \triangle CNB$ (AAS)

II. Short Answer Type Questions

1. In rhombus BEAM, find $\angle AME$ and $\angle AEM$.

[NCERT Exemplar]

Sol. Since diagonals of rhombus bisect each other at right angles (Fig. 3.25)

$$\therefore \angle AOM = 90^\circ$$

In $\triangle AOM$,

$$\angle AOM + \angle OAM + \angle AMO = 180^\circ$$

$$90^\circ + 70^\circ + \angle AMO = 180^\circ$$

$$160^\circ + \angle AMO = 180^\circ$$

$$\angle AMO = 180^\circ - 160^\circ = 20^\circ$$

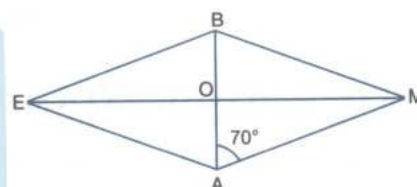
$$\angle AME = \angle AMO = 20^\circ$$

In $\triangle AEM$,

$$AE = AM \quad (\text{Sides of rhombus are equal})$$

$$\angle AME = \angle AEM \quad (\text{Angles opposite to equal sides})$$

$$\therefore \angle AEM = 20^\circ$$



2. In the given parallelogram YOUR (Fig.), $\angle RUO = 120^\circ$ and OY is extended to point S such that $\angle SRY = 50^\circ$. Find $\angle YSR$. [NCERT Exemplar]

Sol. $\angle RYO = \angle RUO = 120^\circ$

(Opposite angles of parallelogram are equal)

$\angle RYS + \angle RYO = 180^\circ$ (Linear pair)

$$\angle RYS + 120^\circ = 180^\circ$$

$$\Rightarrow \angle RYS = 180^\circ - 120^\circ = 60^\circ$$

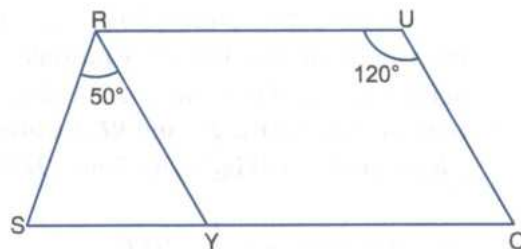
In $\triangle RSY$,

$$\angle YSR + \angle RYS + \angle SRY = 180^\circ$$

$$\angle YSR + 60^\circ + 50^\circ = 180^\circ$$

$$\angle YSR + 110^\circ = 180^\circ$$

$$\angle YSR = 180^\circ - 110^\circ = 70^\circ$$



3. Quadrilateral EFGH is a rectangle in which J is the point of intersection of the diagonals. Find the value of x if $JF = 8x + 4$ and $EG = 24x - 8$. [NCERT Exemplar]

Sol. $EG = 24x - 8$

$$HF = 2(8x + 4) = 16x + 8$$

Since diagonals of rectangle are equal,

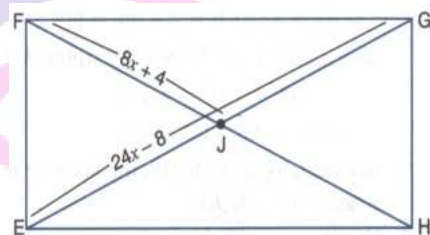
$$\therefore EG = HF$$

$$\text{or } 24x - 8 = 16x + 8$$

$$\text{or } 24x - 16x = 8 + 8$$

$$\text{or } 8x = 16$$

$$\text{or } x = 2$$



4. Find the values of x and y in the adjoining kite. [NCERT Exemplar]

Sol. In the Fig.,

$$m(\angle A) = m(\angle C)$$

But $m(\angle B) = m(\angle D)$ (Property of a quadrilateral i.e., kite)

$$\therefore y = 110^\circ$$

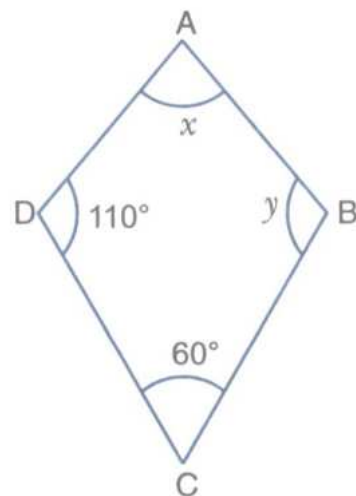
In $\triangle ABCD$,

$$x + y + 60^\circ + 110^\circ = 360^\circ$$

$$x + 110^\circ + 60^\circ + 110^\circ = 360^\circ$$

$$x + 280^\circ = 360^\circ$$

$$x = 360^\circ - 280^\circ = 80^\circ$$



5. Two angles of a quadrilateral are each of measure 75° and the other two angles are equal. What is the measure of these two angles? Name the possible figure so formed.

[NCERT Exemplar]

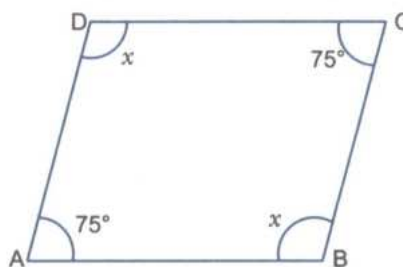
Sol. Let equal angles be x

$$\therefore x + x + 75^\circ + 75^\circ = 360^\circ$$

$$2x + 150^\circ = 360^\circ$$

$$2x = 210^\circ \quad x = 105^\circ$$

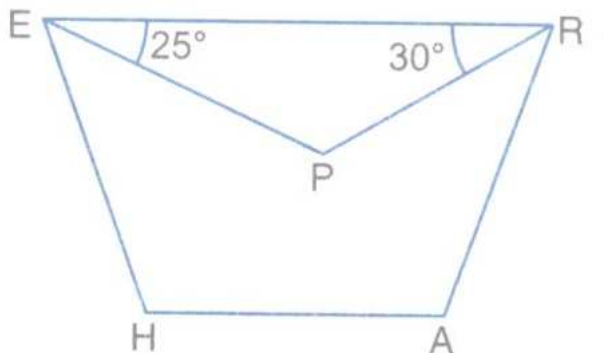
Each equal angle is 105° . The possible figure so formed is parallelogram.



6. In trapezium HARE, EP and RP are bisectors of $\angle E$ and $\angle R$ respectively.

Find $\angle HAR$ and $\angle EHA$.

[NCERT Exemplar]



Sol. Since EP is bisector of $\angle HER$

$$\therefore \angle HEP = \angle PER = 25^\circ$$

$$\angle HER = \angle HEP + \angle PER = 25^\circ + 25^\circ = 50^\circ$$

Now, $ER \parallel HA$ and EH is transversal

$$\angle HER + \angle EHA = 180^\circ \quad (\text{Interior angles on the same side of transversal})$$

$$50^\circ + \angle EHA = 180^\circ$$

$$\angle EHA = 180^\circ - 50^\circ = 130^\circ$$

Since PR is bisector of $\angle ERA$

$$\angle ERA = 2\angle ERP = 2 \times 30^\circ = 60^\circ$$

Also, $\angle ERA + \angle HAR = 180^\circ$ (Interior angles on the same side of transversal)

$$60^\circ + \angle HAR = 180^\circ$$

$$\angle HAR = 180^\circ - 60^\circ = 120^\circ$$



7. In parallelogram MODE, the bisector of $\angle M$ and $\angle O$ meet at Q (Fig.), find the measure of $\angle MQO$.

Sol. MODE is a parallelogram.

$$\angle EMO + \angle DOM = 180^\circ \quad (\text{Interior angles on the same side of transversal})$$

$$\frac{1}{2} \angle EMO + \angle DOM = \frac{1}{2} \times 180^\circ$$

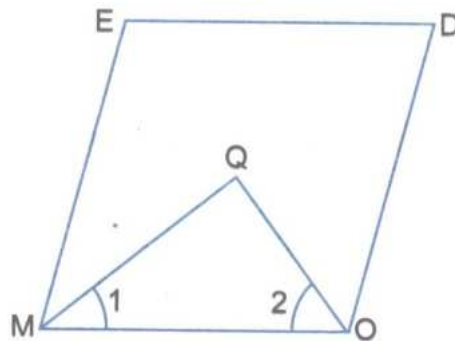
$$\angle 1 + \angle 2 = 90^\circ$$

In $\triangle MOQ$,

$$\angle 1 + \angle 2 + \angle MQO = 180^\circ$$

$$90^\circ + \angle MQO = 180^\circ$$

$$\angle MQO = 180^\circ - 90^\circ = 90^\circ$$



8. A Rangoli has been drawn on a floor of a house. ABCD and PQRS both are in the shape of a rhombus. Find the radius of semicircle drawn on each side of rhombus ABCD.

Measurements are in cm. [NCERT Exemplar]

Sol. Diagonals of rhombus bisect each other at right angle.

$$OA = 2 + 2 = 4 \text{ cm and } OB = 2 + 1 = 3 \text{ cm}$$

In $\triangle AOB$, $\angle AOB = 90^\circ$

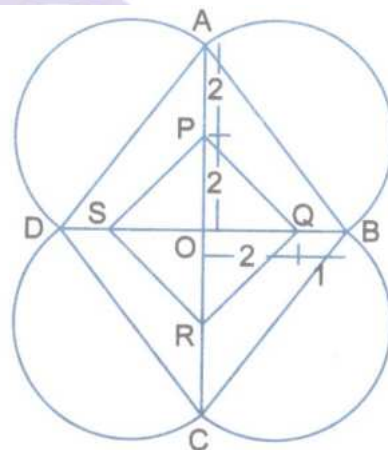
$$\therefore AB^2 = OA^2 + OB^2 \quad (\text{Using Pythagoras theorem})$$

$$= 4^2 + 3^2 = 16 + 9 = 25$$

$$AB = \sqrt{25} = 5 \text{ cm.}$$

This is the diameter of semicircle.

$$\text{Radius} = \frac{5}{2} = 2.5 \text{ cm.}$$



9. The angle between the two altitudes of a parallelogram through the vertex of an obtuse angle of the parallelogram is 45° . Find the angles of the parallelogram.

[NCERT Exemplar]

Sol. Let ABCD is a parallelogram in which $AE \perp BC$ and $AF \perp DC$

In $\square AECF$,

$$\angle AEC + \angle ECF + \angle CFA + \angle EAF = 360^\circ$$

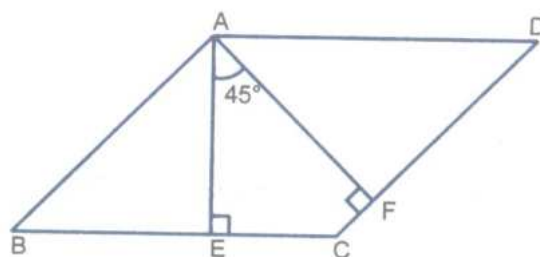
$$90^\circ + \angle ECF + 90^\circ + 45^\circ = 360^\circ$$

$$225^\circ + \angle ECF = 360^\circ$$

$$\angle ECF = 360^\circ - 225^\circ$$

$$\angle ECF = 135^\circ \Rightarrow \angle C = 135^\circ$$

$$\angle A = \angle C = 135^\circ \quad (\text{Opposite angles of parallelogram})$$



$$\angle B + \angle C = 180^\circ \quad (\text{Adjacent angles of parallelogram})$$

$$\angle B + 135^\circ = 180^\circ$$

$$\angle B = 180^\circ - 135^\circ = 45^\circ$$

$$\angle D = \angle B = 45^\circ \quad (\text{Opposite angles of parallelogram})$$

10. In Fig., $FD \parallel BC$ and $AE \parallel AC$. Find the value of x . [NCERT Exemplar]

Sol. In $\triangle ABC$,

$$\angle BAC + \angle ABC + \angle ACB = 180^\circ \quad (\text{Angle sum property})$$

$$52^\circ + 64^\circ + \angle ACB = 180^\circ$$

$$116^\circ + \angle ACB = 180^\circ$$

$$\angle ACB = 180^\circ - 116^\circ = 64^\circ$$

Since $AE \parallel BC$ and AC is transversal,

$$\angle CAE = \angle ACB = 64^\circ \quad (\text{Alternate angles})$$

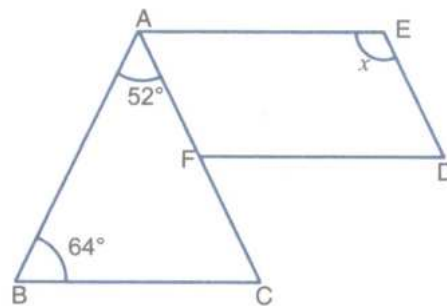
Now, $AE \parallel FD$ and $AF \parallel ED$

\therefore $AEDF$ is a parallelogram.

$$\angle CAE + \angle E = 180^\circ \quad (\text{Adjacent angles of parallelogram are supplementary})$$

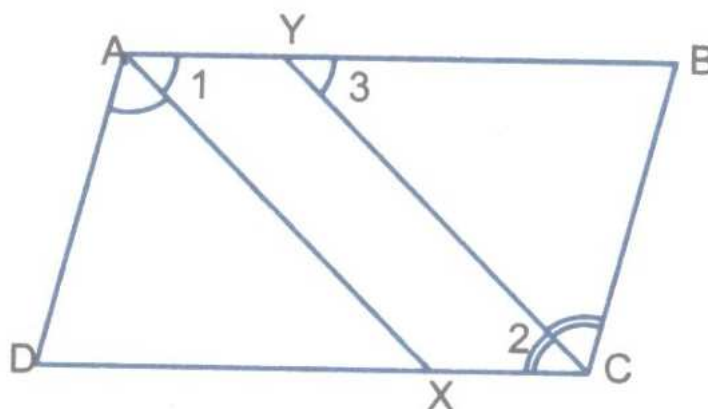
$$64^\circ + x = 180^\circ$$

$$\Rightarrow x = 180^\circ - 64^\circ = 116^\circ$$



11. ABCD is a parallelogram. The bisector of angle A intersects CD at X and bisector of angle C intersects AB at Y. Is AXCY a parallelogram? Give reason.

[NCERT Exemplar]



Sol. $\angle A = \angle C$

(Opposite angles of a parallelogram)

$$\text{or } \frac{\angle A}{2} = \frac{\angle C}{2} \Rightarrow \angle 1 = \angle 2$$

$$\text{But } \angle 2 = \angle 3 \quad (\text{Alternate angles})$$

$$\therefore \angle 1 = \angle 3$$

But they are a pair of corresponding angles

$$\therefore AX \parallel YC \quad \dots(i)$$

$$AY \parallel XC \quad \dots(ii) \quad (\therefore AB \parallel DC)$$

From (i) and (ii)

ΔAXC is a parallelogram.

I. Long Answer Type Questions

1. Two given angles of a parallelogram have equal measure. Find the measure of each of the angles of the parallelogram. [NCERT Exemplar]

Sol. Let ABCD be a parallelogram such that adjacent

$$\text{angles} \quad \angle A = \angle B$$

$$\text{Since,} \quad \angle A + \angle B = 180^\circ$$

$$\Rightarrow \quad 2\angle A = 180^\circ$$

$$\therefore \quad \angle A = \angle B = \frac{180^\circ}{2} = 90^\circ$$

Since, opposite angles of a parallelogram are equal.

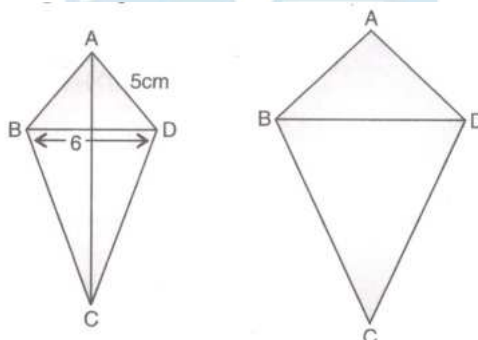
$$\therefore \quad \angle A = \angle C = 90^\circ$$

$$\text{and} \quad \angle B = \angle D = 90^\circ$$

$$\text{Thus,} \quad \angle A = 90^\circ, \angle B = 90^\circ, \\ \angle C = 90^\circ \text{ and } \angle D = 90^\circ$$

2. Construct a quadrilateral ABCD in which $AB = AD = 5$ cm, $BC = CD = 7$ cm and $BD = 6$ cm. What type of quadrilateral is this? [NCERT Exemplar]

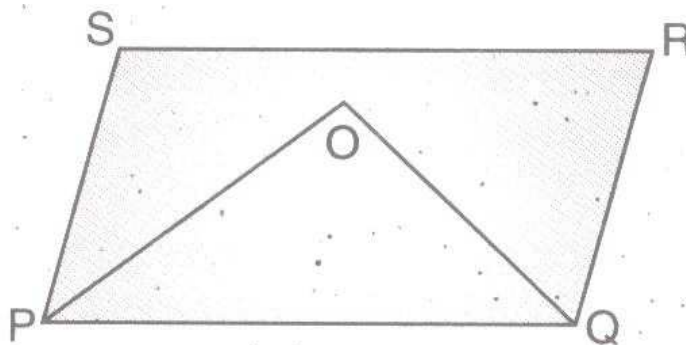
Sol. Looking at the rough figure, draw a line segment $BD = 6$ cm. Taking B and D as centres and 5 cm radius, draw arcs to intersect at the point A, then taking B and D as centres and 7 cm radius, draw arcs in the opposite side of A to intersect at the point C. Join AB, AD and BC, DC. Then ABCD is the required quadrilateral. It is a kite.





3. In a parallelogram PQRS, the bisectors of $\angle P$ and $\angle Q$ meet at O. Find $\angle POQ$.

[NCERT Exemplar]



Sol. Since, OP and OQ are the bisectors of $\angle P$ and $\angle Q$ respectively.

So, $\angle OPQ = \frac{1}{2} \angle P$ and $\angle OQP = \frac{1}{2} \angle Q$

In $\triangle POQ$,

$$\angle OPQ + \angle PQO + \angle POQ = 180^\circ \text{ (Angle sum property)}$$

$$\text{i.e., } \frac{1}{2} \angle P + \frac{1}{2} \angle Q + \angle POQ = 180^\circ$$

$$\text{i.e., } \angle POQ = 180^\circ - \frac{1}{2} (\angle P + \angle Q)$$

$$= 180^\circ - \frac{1}{2} \times 180^\circ$$

$$= 90^\circ$$

4. In a quadrilateral ABCD, DO and CO are the bisectors of $\angle D$ and $\angle C$ respectively.

Prove that $\angle COD = \frac{1}{2} [\angle A + \angle B]$.

[NCERT Exemplar]

Sol. In $\triangle COD$, we have

$$\angle COD + \angle 1 + \angle 2 = 180^\circ$$

$$\Rightarrow \angle COD = 180^\circ - [\angle 1 + \angle 2]$$

$$\Rightarrow \angle COD = 180^\circ - \left[\frac{1}{2} \angle D + \frac{1}{2} \angle C \right]$$

$$\Rightarrow \angle COD = 180^\circ - \frac{1}{2} [\angle D + \angle C]$$

$$\text{But } \angle A + \angle B + \angle C + \angle D = 360^\circ$$

$$\Rightarrow \angle C + \angle D = 360^\circ - (\angle A + \angle B)$$

$$\Rightarrow \angle COD = 180^\circ - \frac{1}{2} [360^\circ - (\angle A + \angle B)]$$

$$= 180^\circ - \frac{1}{2} [360^\circ] + \frac{1}{2} [\angle A + \angle B]$$

$$= 180^\circ - 180^\circ + \frac{1}{2} [\angle A + \angle B]$$

$$= \frac{1}{2} (\angle A + \angle B)$$

$$\text{Thus, } \angle COD = \frac{1}{2} [\angle A + \angle B]$$



II. Long Answer Type Questions

1. In rectangle READ (Fig.), find $\angle EAR$, $\angle RAD$ and $\angle ROD$.

[NCERT Exemplar]

Sol. We have,

$$\angle EOR + \angle EOA = 180^\circ \text{ (Linear pair)}$$

$$60^\circ + \angle EOA = 180^\circ$$

$$\angle EOA = 180^\circ - 60^\circ = 120^\circ$$

Since diagonals of a rectangle are equal and they bisect each other, therefore, in $\triangle EOA$ we have

$$OE = OA \Rightarrow \angle 1 = \angle 2$$

(Angles opposite to equal sides)

In $\triangle EOA$

$$\angle 1 + \angle 2 + \angle EOA = 180^\circ$$

(Angle sum property)

$$2\angle 2 + 120^\circ = 180^\circ$$

\Rightarrow

$$2\angle 2 = 60^\circ \quad \angle EAR = 30^\circ$$

$$2\angle 2 = 60^\circ$$

\Rightarrow

$$\angle 2 = 30^\circ$$

$$\angle EAR + 120^\circ$$

Since each angle of a rectangle is a right angle,

$$\angle EAD = 90^\circ$$

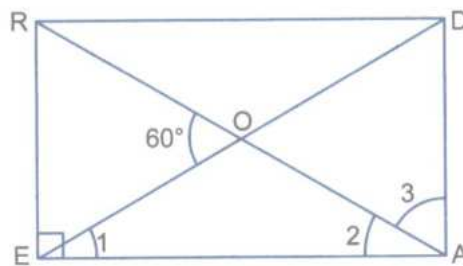
$$\angle 2 + \angle 3 = 90^\circ$$

$$\Rightarrow 30^\circ + \angle 3 = 90^\circ$$

$$\angle 3 = 90^\circ - 30^\circ = 60^\circ$$

$$\angle RAD = 160^\circ$$

Now, $\angle ROD = \angle EOA = 120^\circ$ (Vertically opposite angles)



2. In parallelogram PQRS, O is the midpoint of SQ (Fig.). Find LS, LR, PQ, QR and diagonal PR.

[NCERT Exemplar]

$$\text{Sol. } \angle PQR + \angle RQY = 180^\circ \text{ (Linear pair)}$$

$$\angle PQR + 60^\circ = 180^\circ$$

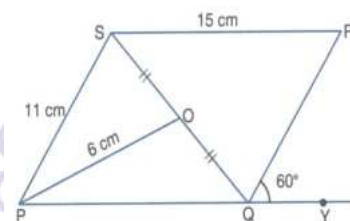
$$\angle PQR = 180^\circ - 60^\circ = 120^\circ$$

$$\text{Now, } \angle S = \angle PSR = \angle PQR = 120^\circ$$

(Opposite angles of parallelogram are equal)

Again, $\angle PQR + \angle R = 180^\circ$ (Adjacent angles of parallelogram)

$$120^\circ + \angle R = 180^\circ$$





$$\angle R = 180^\circ - 120^\circ = 60^\circ$$

$PQ = SR = 15 \text{ cm}$ (Opposite sides of parallelogram are equal)

$$QR = PS = 11 \text{ cm}$$

Diagonal $PR = 2(PO)$ (Diagonals of a parallelogram bisect each other)

$$= 2 \times 6 = 12 \text{ cm}$$

3. In parallelogram **LOST**, (Fig.) $SN \perp OL$ and $SM \perp LT$. Find $\angle STM$, $\angle SON$ and $\angle NSM$

[NCERT Exemplar]

Sol. $\angle SMT = 90^\circ$

$$\angle MST = 40^\circ \text{ (Given)}$$

In $\triangle STM$,

$$\angle SMT + \angle MST + \angle STM = 180^\circ$$

$$\text{(Angle sum property)} \quad 90^\circ + 40^\circ + \angle STM = 180^\circ$$

$$130^\circ + \angle STM = 180^\circ$$

$$\angle STM = 180^\circ - 130^\circ = 50^\circ$$

$$\angle SON = \angle STM = 50^\circ \text{ (Opposite angles of parallelogram)}$$

In $\triangle OSN$,

$$\angle OSN + \angle ONS + \angle SON = 180^\circ \text{ (Angle sum property)}$$

$$\angle OSN + 90^\circ + 50^\circ = 180^\circ$$

$$\angle OSN + 140^\circ = 180^\circ$$

$$\angle OSN = 180^\circ - 140^\circ = 40^\circ$$

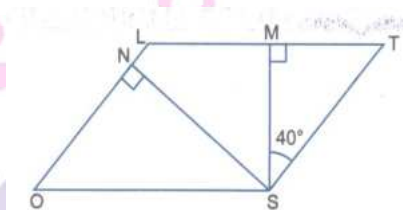
Now,

$$\angle SOL + \angle OST = 180^\circ \text{ (Adjacent angles of parallelogram)}$$

$$50^\circ + 40^\circ + \angle NSM + 40^\circ = 180^\circ \text{ (}\angle OST = \angle OSN + \angle NSM + \angle MST\text{)}$$

$$130^\circ + \angle NSM = 180^\circ$$

$$\angle NSM = 180^\circ - 130^\circ = 50^\circ$$



4. A diagonal of a parallelogram bisects an angle.

[NCERT Exemplar]

(i) Will it also bisect the other angle?

(ii) Is it a rhombus? Give reason.

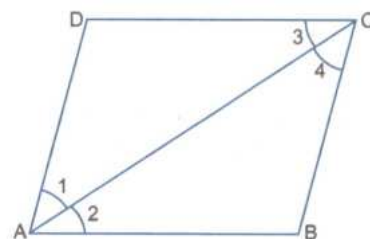
Sol. Let ABCD be a parallelogram (Fig. 3.39) in which

$$\angle 1 = \angle 2$$

(i) $\angle 1 = \angle 4$ (Alternate angles)

and $\angle 2 = \angle 3$ (Alternate angles)

But $\angle 1 = \angle 2$





$$\therefore \angle 3 = \angle 4$$

So, the diagonal will bisect the other angle.

$$(ii) \angle 1 = \angle 2 \quad (\text{Given})$$

$$\angle 2 = \angle 3 \quad (\text{Alternate angles})$$

$$\angle 1 = \angle 3$$

Hence, $CD = DA$ (Sides opposite to equal angles are equal)

\therefore ABCD is a rhombus.

I. High Order Thinking Skills [HOTS] Questions.

1. (a) Prove that the interior angle of a regular pentagon is three times the exterior angle of a regular decagon.

(b) Is rectangle a regular polygon? Why?

Sol. (a) We know that,

A pentagon has five sides, then $n = 5$

But each interior angle of a regular polygon $= \left(\frac{n-2}{n}\right) \times 180^\circ$

$$\therefore \text{Each interior angle of a regular pentagon} = \left(\frac{3}{5}\right) \times 180^\circ$$

$$= 3 \times 36 = 108^\circ$$

and a decagon has 10 sides, then

$$\text{Exterior angle of a regular decagon} = \left(\frac{360^\circ}{180^\circ}\right) = 36^\circ$$

Therefore, interior angle of regular pentagon

$$= 3 \times \text{The exterior angle of a regular decagon}$$

$$= 3 \times 36^\circ = 108^\circ$$

- (b) Yes, a rectangle is not a regular polygon because it is equiangular but not all sides are equal.

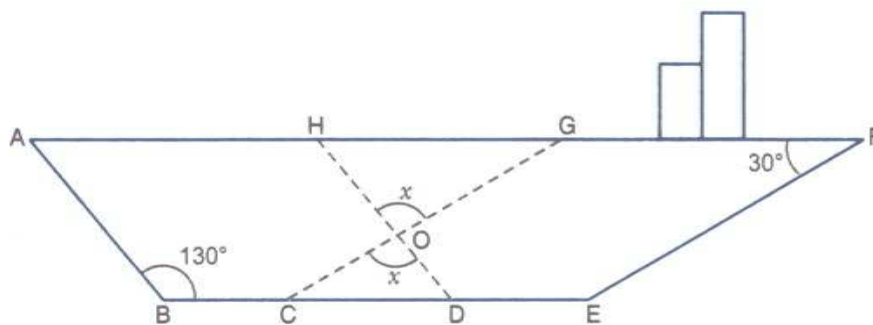
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II. High Order Thinking Skills [HOTS] Questions.

1. In Fig. a ship, $ABDH$ and $CEFG$ are two parallelograms. Find the value of x .

[NCERT Exemplar]



Sol. Since $ABDH$ is a parallelogram,

$$\angle B + \angle BDH = 180^\circ$$

(Adjacent angles of parallelogram are supplementary)

$$130^\circ + \angle BDH = 180^\circ$$

$$\angle BDH = 180^\circ - 130^\circ = 50^\circ$$

Similarly, $CEFG$ is a parallelogram.

$$\angle GCE = \angle F = 30^\circ$$

In $\triangle COD$,

$$\angle OCD + \angle ODC + \angle COD = 180^\circ \text{ (Angle sum property)}$$

$$\angle GCE + \angle BDH + x = 180^\circ$$

$$30^\circ + 50^\circ + x = 180^\circ$$

$$80^\circ + x = 180^\circ$$

$$x = 180^\circ - 80^\circ = 100^\circ$$

2. $ABCDE$ is a regular pentagon. The bisector of angle A meets the side CD at M (Fig.).

Find $\angle AMC$ [NCERT Exemplar]

Sol. The measure of each interior angle of regular pentagon = 108°

$$\therefore \angle MAB = \frac{1}{2} \times 108^\circ = 54^\circ$$

In $\triangle ABCM$,

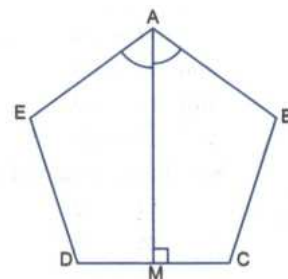
$$\angle MAB + \angle ABC + \angle BCM + \angle AMC = 360^\circ$$

(Sum of angles of a quadrilateral is 360°)

$$54^\circ + 108^\circ + 108^\circ + \angle AMC = 360^\circ$$

$$270^\circ + \angle AMC = 360^\circ$$

$$\angle AMC = 360^\circ - 270^\circ = 90^\circ$$



3. ABCD is a rhombus such that the perpendicular bisector of AB passes through D

(Fig.). Find the angles of the rhombus.

[NCERT Exemplar]

[Hint : Join BD. Then AABD is equilateral.]

Sol. Let ABCD be a rhombus in which DE is perpendicular bisector of AB. Join BD. (Fig.) In $\triangle ADE$ and $\triangle BDE$

$$AE = EB$$

(DE is perpendicular bisector of AB)

$$DE = DE \quad (\text{Common})$$

$$\angle AED = \angle BED \quad (\text{Each } 90^\circ)$$

$$\triangle ADE = \triangle BDE \quad (\text{SAS})$$

$$AD = BD \quad (\text{CPCT})$$

So, AABD and ABCD are equilateral.

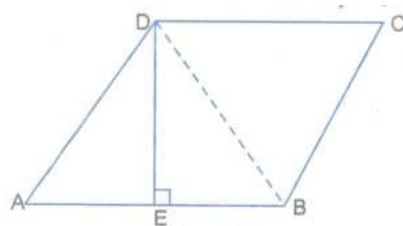
$$\angle A = \angle C = 60^\circ \quad (\text{All angles of equilateral triangle are } 60^\circ)$$

Now, $\angle A + \angle D = 180^\circ$ (Adjacent angles are supplementary)

$$60^\circ + \angle D = 180^\circ$$

$$\angle D = 180^\circ - 60^\circ = 120^\circ$$

Hence, $\angle A = \angle C = 60^\circ$ and $\angle B = \angle D = 120^\circ$.



4. A regular pentagon ABCDE and a square ABFG are formed on opposite sides of AB.

(Fig.) Find $\angle BCF$.

[NCERT Exemplar]

$$\begin{aligned} \text{Sol. Each interior angle of regular pentagon} &= \frac{(2 \times 5 - 4)}{5} \times 90 \\ &= \frac{(10 - 4) \times 90}{5} \times 108^\circ \end{aligned}$$

Since ABFG is a square,

$$\text{So, } \angle ABF = 90^\circ$$

Therefore,

$$\angle CBF = 360^\circ - (108^\circ + 90^\circ)$$

$$\angle CBF = 360^\circ - 198^\circ = 162^\circ$$

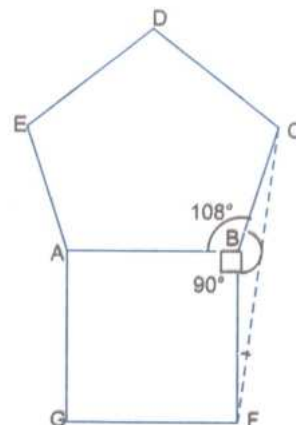
$$AB = BF$$

(All sides of square are equal)

$$AB = BC$$

(All sides of regular pentagon are equal)

$$\therefore \quad BF = BC \quad \dots(i)$$





In $\triangle CBF$,

$$FB = BC \quad (\text{From (i)})$$

$$\angle CFB = \angle BCF = x$$

(Angles opposite to equal sides)

$$\therefore x + x + 162^\circ = 180^\circ$$

$$2x = 180^\circ - 162^\circ$$

$$2x = 18^\circ \Rightarrow x = 9^\circ$$

$$\therefore \angle BCF = 9^\circ$$

I. Value Based Questions.

1. (a) The four angles of a quadrilateral are as 3 : 5 : 7 : 9. Find the angles.
 (b) Is an equilateral triangle a regular polygon? Why?

Sol. (a) Let $\angle A = 3x$, $\angle B = 5x$, $\angle C = 7x$ and $\angle D = 9x$

We know that, in a quadrilateral

$$\angle A + \angle B + \angle C + \angle D = 360^\circ$$

$$\text{Then, } 3x + 5x + 7x + 9x = 360^\circ$$

$$\text{or } 24x = 360^\circ$$

$$\text{or } x = \frac{360^\circ}{24} = 15^\circ$$

Therefore,

$$\angle A = 3x = 3 \times 15^\circ = 45^\circ$$

$$\angle B = 5x = 5 \times 15^\circ = 75^\circ$$

$$\angle C = 7x = 7 \times 15^\circ = 105^\circ$$

and

$$\angle D = 9x = 9 \times 15^\circ = 135^\circ$$

- (b) Yes, an equilateral triangle is a regular polygon because it is both equiangular and equilateral.

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